

Teacher's Guide for **The Math Behind Our Democracy:** Gerrymandering

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Workshop Description

Who gets a say in democracy? How do politicians get to pick their voters? When district maps are drawn after every census, they are sometimes designed to benefit one party. Sometimes this allows a minority of voters to elect a majority of seats, like in the map on the far right. In the process, gerrymandering creates voting districts that look more like an inkblot test than a real map. In this workshop, you'll find a way to quantify gerrymandering based on both the shapes of districts and how much the outcome of an election differs from the actual votes cast.



Workshop Requirements

- > Time: 55 minutes (or more)
- > Materials: Access to computers with google sheets, slides, docs, and ability to download files.
- Suggested ages: 7th-12th grade
- Students should know: how to use google apps



Learning Goals

- > Understand that very simple math can have great consequences
- > Learn how to quantify compactness by analyzing shapes
- > Learn how to quantify fairness by comparing voting data with election data
- > Gain interest in representation and voting issues

Preparation for Gerrymander Activity

Make a form like <u>this one</u> for the live gerrymandering activity. You can ask the students what are some contentious issues for them (they should be light-hearted, like the ones in the template). There should be at least 3-4 topics to vote on - you will choose the topic where the results are easiest to gerrymander.

Have the students fill out the form beforehand (ideally during the previous class). Have them write down their answers so they don't forget. It is important that everyone has filled it out before you do the next step.

Open up the responses in a spreadsheet using the finise to the top right of the form. Now choose a voting topic to gerrymander. A good target is one that is split roughly 1/3 to 2/3. Copy the columns with the student names and the chosen voting topic over into a blank area of the spreadsheet. Then rearrange the students and their votes by cutting and pasting them into groups.

A couple of tips:

- Always copy the student name and their vote together and move them at the same time.
- Aim for district sizes of 3, 5, or 7 students each. Also aim to have an odd number of districts. It's okay if the districts aren't all the same size (it is better if they are similarly sized in case students want to see the details behind the scenes, but you don't need them to be exactly the same size).
- Try to pack and crack: Make some districts where everyone votes the same way, and the rest of the districts where the vote is narrowly won.
- If it isn't working out, try starting over using a different topic the numbers will be different.



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At the start of class, you will put the students into groups or breakout rooms based on the districts you created, then have each group report out the majority student vote for their district.

Your objective with creating the districts is to skew the results to demonstrate the impact that gerrymandering can have. It is especially powerful if you can take the minority of student votes and make them win the majority of districts! If the student votes are evenly split, you should be able to make one side win in a landslide.

Preparation for Map Tiling Activity

For the map tiling activity, the objective is to demonstrate how students can estimate the area of complex shapes to measure the compactness of voting districts. The measure of compactness we will use is the ratio of the surface area of the district to the area of the smallest circumscribed circle around the district.

Before class, make a copy of the <u>Gerrymandered Or Not?</u> slide deck and share with students the new URL (change permissions so that anyone can edit). Each student will take one slide or create a copy of one to work on. For the demonstration, follow the guide below to create shapes in google slides (you want to make the shapes transparent and have a thick border so you can see the district underneath). The students will then do the same thing for a district of their choosing.





First, draw the smallest circle that encompasses the entire district. If you hold shift you will make sure to draw a circle, instead of an oval.

Then start covering over the district using basic shapes. Here, it takes 7 shapes to adequately cover Ohio's 9th district. The more shapes it requires, the less compact it is, and the more likely it is to be a gerrymandered district.

Then move the shapes into one portion of the circle to visualize what fraction of the circle the district actually takes up. Here, Ohio's 9th district takes up probably a tenth of the circle's area. This district is not very compact, which suggests it may be gerrymandered.

Presentation Notes



Short Game to get students excited about the topic. Tell them you're about to show them 4 different shapes for each one you want them to call out what the shapes remind them of. Then on the last slide you'll reveal that each shape was the mirrored image of a voting district in America and how they look so odd



The second secon	because of Gerrymandering which is the topic of today.
Gerrymandering What is it? • When a political party draws the boundaries of legislative districts in a way that favors them. • It's othen said gerrymandering is a way for elected officials to pick their voters instead of voters getting to choose their elected officials.	Read through the bullets to help give students a better definition of what gerrymandering is.
Occurrymandering Some examplesOrder are simplesOrder are simples<	Share these examples with the class and point out the odd shapes like the long skinny one and purple spiral. The reason many districts are shaped this way is to include bits and pieces of different cities that are spread out geographically. So you get skinny lines connecting cities and large bulges near population centers.



What state do you think gerrymandering started in? Why do you think it's called gerrymandering?	Ask the students these questions and have them call out guesses. The answer to the first is Massachusetts. The answer to the second is explained on the next slide.
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How do we quantify how Cerrymandered a district is? • This is actually still hotly debated. • The Supreme Court in 2019 said to evaluate partisan gerrymandering they needed a "limited and precise standard" that would be "clear, manageable, and politically neutral" but no one has proposed one.	It is important to emphasize that people are working on inventing this math right now! People are currently working on how to determine if a district is gerrymandered or not. While gerrymandering is deemed unconstitutional, people still need to figure out ways to quantify what it means for a district to be gerrymandering, for a case to be able to stand up in a court.
How do we quantify how Gerrymandered a district is? Method H • Ve can use geometry of dermine "compactness" • Look at perimeter of the district vs. its surface area. • Draw a circle around the district vs. its surface area then calculate the surface area of the district and compare.	The first method we'll cover is compactness. The launch for the activity is on the next slide. Here, you should do a demo of the activity, following the steps in the Preparation section. In advance, make a copy of the <u>Gerrymandered Or Not?</u> slide deck and share with students the new URL (change permissions so that anyone can edit).
Activity Let's quantify compactness	Now you have students get onto the shared google slide deck and do the compactness activity for their own district. You can monitor their progress by scrolling through the slide deck. You may have to help troubleshoot. If there are not enough slides for every student, or if they want to do multiple, they can make a copy of another slide.
	When they're done, screenshare as you go through each slide in the presentation. Point out districts that are especially compact or not compact, and relate this to gerrymandering: if a district is not very compact, it usually means a politician had to work hard to shape it that way in order to manipulate who their voters



	were. Districts that are long and skinny and have a small district to circle area ratio are usually a sign of gerrymandering.
	This is a good time for a break
Your Voting Districts Enter your breakout room and we will come and tally your votes. Breakout District 1: Name A, Name B, Name C Breakout District 2: Name A, Name B, Name C Breakout District 3: Name A, Name B, Name C	Here is where you announce the districts you placed them in after they "registered" Refer to the first part of the Preparation section. Have the students go into their districts, either by assigning them to breakout rooms or having them go to different tables.
The Results Drum roll please.	Go around and collect the votes from the districts (each person casts their vote but the district is won by the option that got the majority of votes in the district). One way to display the results is to enter each district's vote into a new google form, then view the pie chart in the responses.
Entropy Constraints of the second sec	Show your students the two pie charts. The first is from the class registration showing the true breakdown of the class. The second is from your distinct voting and will show how you were able to shift the power. This demonstrates gerrymandering in real time.
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PROCEEDIngs AbaD CREACHING Dry on with a geny modes 10 dates take fuels 500 prix varies and 500 prix to service the nederal dates with by pack approximations the service of the service	Walk them through this example and highlight the packed and cracked districts (it is explained on the slide).



<text><list-item><list-item><list-item><list-item></list-item></list-item></list-item></list-item></text>	Walk them through the example. For each district, the number of votes in excess of the 50% needed to win are counted as wasted votes, as well as all of the votes on the losing side. In this example, our packed district has 45 wasted green votes and only 5 wasted pink votes. In the cracked districts there are again 45 wasted green votes and only 5 wasted pink votes. Packing and cracking is a strategy to maximize the number of the opposition's votes that are wasted. It's important to emphasize that the term "wasted votes" is academic lingo, and no person's vote should ever be considered wasted as it can still have a big impact on the election
Gerrymander the Game http://gametheorytest.com/gerry/game/	Now open up this game and walk through how to play with the students showing them when they should pack a district and when they should crack a district. Then give them the link and let them play.
How do we quantify how Cerrymandered a district is? • Simulation algorithms • We can create programs that produce MANY different maps and then run these other calculations on them and see how they compare to the original map. • One simulation looking at a map in Maryland found after drawing 250 million possible maps the proposed map favored Democrats more than 98.79% of the maps drawn by the algorithm.	There are more ways to determine if a district is likely to be gerrymandered. You can pique their interest by introducing another method, which is using algorithms. You could extend this workshop by designing an activity for this method.
How it's done Who & When • Who: State Legislatures • When: after each census when new districts are drawn • Redistricting will be taking place this year!	End the class by telling the students who has this power in real life (local and state legislatures), and emphasize how issues about representation and gerrymandering are decided at the local level, which means that local elections are extremely important.

Please use these materials and tailor them to your students!

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